The aim of this paper is to scrutinize the mixed convective flow of Williamson nanofluid in the presence of stretched surface with various physical effects. The impact of Brownian motion and thermophoresis is the part of this investigation. In addition, the features of thermal radiations is considered in energy equation for motivation of problem. Theory of the microorganism is used to stable the model. Mathematical modelling is carried out. Appropriate similarity functions are used to transform the couple of governing PDEs into set of ODEs. Wolfram MATHEMATICA is engaged to solve transformed equations numerically with the help of shooting scheme. The influence of emerging flow parameters like magnetic, thermophoresis, porosity, Péclet and Lewis number on the velocity, temperature, volumetric concentration and density of microorganism distribution are presented in tables and graphs.

Keywords: Gyrotactic Microorganism; Williamson nanofluid; MHD; Bioconvection; Shooting method.

FACS: 44.10.+i, 44.05.+e, 44.30.+v, 47.10.ad.

1. INTRODUCTION

Fluid mechanics have two principal types of fluids called Newtonian and non-Newtonian fluid flow belongings of Newtonian and non-Newtonian fluids are not similar. Newtonian fluids are those which satisfy Newton law of viscosity like water, glycerol, alcohol and benzene. Here, the contact between strain rates is explained by taking out the basic model, especially for such liquids that do not obey the Newton law of viscosity. Fluids like toothpaste, cosmetics, butter, ketchup, custard, shampoo, blood, honey, paint are the examples of non-Newtonian fluids in daily life. Because of the complicated and interdisciplinary nature, the study of non-Newtonian fluids has recently involved a lot of attention from researchers. Nanofluids are small-sized solid particles dissolved in conventional processing fluids. Water, glycerol, engine oils, ethylene glycol, and pump oil are conventional processing fluids. Nanoparticles, which are normally recycled in nanofluids are made from various materials, such as metals or non-metals. Choi and Eastman [1] found that by suspending metallic nanoparticles in traditional fluids, the resulting nanofluids have predicted high thermal conductivity. The movement of heat transfer in a fluid will enhance the conduction and convection coefficients. Nanofluid research is becoming more important and effective. Nanofluids are developed to achieve maximal thermal properties at the smallest concentration possible. The production of nanofluids resulted in increased thermal conductivity and improved heat transfer properties. The transmission qualities and heat conduction characteristics of the base fluids, such as organic, refrigerant, and ethylene liquids, are altered by all non-metallic and metallic particles. In fact, while higher thermal conductivity is dependent on nanoparticles, the efficacy of heat transfer enhancement is also dependent on scattered particles, material type, and other parameters. Using additives to improve a base fluid's heat transfer capacity is another option. Nanofluids have a wide variety of applications and they can be used in different sectors, including heat transferring and other cooling applications. In the biological and biomedical sectors, nanofluids have played vital roles for a long time, and their use will be extended to growth. Nanofluids have also been used as detergents and smart fluids. Jawad et al. [2] has inspected that nanofluid is such kinds of hotness move source having nano-particles with shape short 100 (nm). Wen and Ding [3] have found that nanofluids significantly improved convective heat transfer, according to the findings. The improvement was especially noticeable in the entrance region, and it was much greater than the increase in thermal conduction. The classical Such equation was also shown to be ineffective in predicting the heat transfer conduct of nanofluids. The main explanations were proposed to be nanoparticle migration and the commotion of the boundary layer. Bhattacharyya et al. [4] have evaluated the thermal conductivities of aluminium oxide-water nanofluids at different temperatures and clarify that the enhancement in thermal conductivity is temperature dependent.

Magnetohydrodynamics, also known as hydro-magnetics, is the learning of dynamics of the existence of magnetic properties and the liquid effects that are electrically conducted. Salt water, liquid metals, plasma and electrolytes are known examples of magneto fluids. Alfvén [5], a Swedish physicist, was the first to introduce the MHD fluid flow. Turkyilmazoglu [6] has calculated analytically the magnetohydrodynamic flow and thermal transport features of nanofluid flow across a continually extending or contracting permeable sheet in the presence of temperature and velocity
slip. Qayyum et al. [7] have observed analytical treatment of MHD radiative flow of tangential hyperbolic nanofluid under the impact of heat generation or absorption. The study's reproduction was based on Newtonian heat and mass conditions. Mohyud-Din et al. [8] have presented a revised model for Stokes first issue in nanofluids. At the boundary, this model considers a zero-flux condition. Following the implementation of the similarity transforms, the governing equations were altered into a system of non-linear ordinary differential equations. Majeed et al. [9] has concentrated that Magnetohydrodynamics manages electrically led liquid having attractive properties in like manner of electrolytes, salt water, plasmas, and fluid metals. Nadeem et al. [10] have studied the Casson fluid's MHD boundary layer movement across an increasingly permeable shrink sheet.

Williamson [11] concentrated on the progression of pseudoplastic materials and fostered a model to clarify the progression of liquids and gave trial results. In the Williamson model, the compelling consistency ought to be decreased endlessly by raising the shear rate, which is boundless thickness very still and no consistency as the shear rate approaches endlessness. The Williamson liquid model is an essential reenactment of non-Newtonian liquid viscoelastic shear diminishing highlights. Hayat et al. [12] have analysed the results of chemically reactive flow of nanomaterial based on Brownian and Thermophoresis movement with a nonlinear bidirectional stretching layer with a constant thickness. Williamson fluid rheological expressions and the optimal homotopy analysis approach were used. Zaman and Gul [13] have examined in the presence of Newtonian conditions, the magnetohydrodynamic (MHD) of Williamson nanofluid bioconvective flow containing microorganisms. The bvp4c technique is used to achieve numerical solutions. Danish et al. [14] have explained a new numerical model to analyse the features of activation energy on magnetized Williamson fluid over a section with nonlinear thermal radiation. The Brownian and thermophoresis nanofluid properties have been described using the Buongiorno model. For more details see Refs [15-23].

Kuznetsov [24] were the first to investigate the topic of bioconvection in a suspension containing small solid particles (nanoparticles). To see how minor particles that are denser than water affect the permanence of a motile gyrotactic bacteria suspension in a finite-depth horizontal fluid layer. Bioconvection has the potential to improve mass transport and mixing, particularly in microvolumes, as well as the stability of nanofluids. Thus, a nanofluid and bioconvection combination could be promising for new microfluidic devices. Khan et al. [25] have explained the movement over a permeable wedge in the occurrence of viscous dissipation and Joule heating. The nanofluid containing gyrotactic microorganisms was expected to be saturated in the wedge under the effect of magneto-hydrodynamics. The passive control model was used to formulate the problem. Uddin et al. [26] have evaluated numerically the impacts of bioconvection on fluid velocity and thermal slips over the flow of nanofluid passing through the horizontal touching sheet. They introduced the first time-similarity solution to nano-bioconvection. The influences of velocity, the bioconvection Lewis number, Peclet number and the bioconvection Peclet number on the governing equations, including local wall mass flux and local Nusselt number, were discussed. Naz et al. [27] have reviewed Cross nanofluid with gyrotactic germs, entropy formation and heat and mass transmission. The solutions were obtained using the optimal homotopy analysis technique, and the most important consequences were discussed graphically and numerically. The geometry of flow model is presented in Fig. 1 as:

![Figure 1. Geometry of physical model](image.png)

2. PROBLEM STATEMENT

A mathematical study of MHD flow of an incompressible Williamson nanofluid is presented. The two-dimensional fluid flow is passing through porous media and stretched surface. Aman et al. [28] work of mixed convection nanofluid flow with gyrotactic microorganisms over extending plate has been considered. The first step is to explore this work and then extending that by observing the consequence of magnetic field, thermal radiation and chemical reaction with compactness of motile microorganisms.
The governing equations [29] are:

\[ u_x + v_y = 0 \]  
(1)

\[ u u_x + v u_y = \nu u_{yy} - \frac{\alpha B^2 u}{\rho_f} + \Gamma u u_y \]  
(2)

\[ u T_x + v T_y = \frac{k}{(pc_f)} \left( T_y \right) + \frac{(pc_f)}{(pc_f)} \left( \frac{D_T}{T_m} \right) T_y^2 + D_s C_y \]  
(3)

\[ u C_y + v C_y = D_s C_y + \frac{D_s}{T_m} T_y - K_0 (C - C_\infty) \]  
(4)

\[ u w_x + v w_y + \frac{h \nu}{C_w - C_\infty} \left[ \eta, C_y \right] = D_s n_y \]  
(5)

Conditions:

The initial and boundary conditions [30] are:

\[ v = v_0, u = \lambda U_y, T = T_\infty, C = C_\infty, N = N_\infty \text{ at } y = 0, \]
\[ u \to 0, T \to T_\infty, C \to C_\infty, N \to N_\infty \text{ as } y \to \infty. \]  
(6)

Similarity transformations:

\[ u = b x f' (\eta); \quad v = -(b u) f' (\eta); \quad \eta = \sqrt{\frac{2}{\nu \gamma}} \gamma; \quad \phi (\eta) = \frac{C - C_\infty}{C_\infty - C_\infty}; \quad \chi (\eta) = \frac{N - N_\infty}{N_\infty - N_\infty}; \quad \theta (\eta) = \frac{T - T_\infty}{T_\infty - T_\infty}. \]

3. NUMERICAL SCHEME: SHOOTING METHOD

The physical aspect of the flow problem under consideration has been investigated by solving the final set of equations, namely (2) to (5) associated with the new boundary conditions (6). The policy of shooting method is specified as next (Fig. 2). The higher order derivatives in the above mentioned are reduced to first order as follows:

\[ f''' (\eta) + \lambda f'' (\eta) f' (\eta) + f'' (\eta) f (\eta) - f' (\eta) - M f'' (\eta) = 0, \]  
(7)

\[ \theta'' (\eta) + Pr f (\eta) \theta' (\eta) - 2 Pr \theta (\eta) + \frac{Nc}{(Le)(Nbt)} \phi' (\eta) \theta (\eta) + \frac{Nc}{(Le)(Nbt)} \theta^2 (\eta) = 0, \]  
(8)

\[ \phi'' (\eta) + \frac{1}{Nbt} \theta'' (\eta) + Sc f (\eta) \phi' (\eta) - Sc \gamma \phi (\eta) = 0, \]  
(9)

\[ \chi'' (\eta) + Sc f (\eta) \chi' (\eta) - Pe \chi (\eta) \phi' (\eta) + (\chi (\eta) + \sigma) \phi'' (\eta) = 0. \]  
(10)

The higher order equation from (7) to (10) are reduced to first order as:

\[ f' = u, \quad u' = v, \quad \theta' = w, \quad \phi' = q, \quad \chi' = g, \]
\[ v' (1 + \lambda v) + v f - u^2 - \mu u = 0, \]  
(11)

\[ w' + Pr f w - 2 Pr \theta + \frac{Nc}{Le} q w + \frac{Nc}{(Le)(Nbt)} w^2 = 0, \]  
(12)

\[ q' + \frac{1}{Nbt} w' + Sc f q - Sc \gamma \phi = 0, \]  
(13)

\[ g' + Sc f g - Pe [q g + (\chi + \sigma) q' (\eta)] = 0. \]  
(14)

The transformed linearly boundary condition follows that

\[ f (0) = S, \quad f' (0) = \Lambda, \quad \chi (0) = 1, \theta (0) = 1 \]
\[ f'' (0) = 0, \theta = 0, \phi = 0, \chi = 0 \text{ as } \eta \to \infty. \]  
(15)

The dimensionless drag force factor \( C_f = \frac{2 \tau_s}{\rho_f u_0^2} \), the Nusselt amount \( Nu_x = \frac{x \tau_s}{\alpha (T_m - T_\infty)} \), local Sherwood amount...
\[ S_{h_x} = \frac{x_q}{d_h(C_{w0} - C_{in})} \] and density of microorganism’s amount \( N_{n_x} = \frac{x_q n}{d_n(n_{w0} - n_{in})} \) on the surface in x -direction are given by

\[ (Re_x)^{1/2} f'(0) = \left[ f''(0) + \frac{We}{2} f'^2(0) \right], \quad (Re_x)^{-1/2} Nu_x = -\theta'(0), \quad (Re_x)^{-2} Sh_x = -\phi'(0), \quad (Re_x)^{-1/2} N n_x = -\chi'(0) \tag{16} \]

Here is \( Re_x \) the Reynolds amount.

![Figure 2. Chart of shooting method steps.](image)

### 4. CODE VALIDATIONS

Table 1 provides a critical study of the current findings of \(-\theta'(0)\) and \(-\phi'(0)\) for the Brownian motion parameter \( N_{bt} \) utilizing the bvp4c. The critical study of these numerical findings in Table 1 reveals that the scheme is valid, \( M = 0.5, \lambda = 0.1, \Pr = 7, \text{Ne}=\sigma = 0.3, \text{Pe} = \text{Le} = \text{Sc} = 0.2 \) and \( \gamma = 0 \). The comparison of findings in Table 1 shows the astonishingly considerable arrangements of the current inquiry with the bvp4c results, which motivates the author to tackle this problem with changes of thermal radiation and chemical reaction effects using a well-known shooting approach.

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### 5. RESULT AND DISCUSSION

In the current investigation we analyzed the impact of different parameters graphically on non-layered speed, non-layered liquid temperature, dimensionless liquid focus, and non-layered motile microorganism profiles. The principal request arrangement of conditions along with limit and starting conditions is tackled by utilizing the order ND settled on Mathematica. For this, fixed upsides of certain boundaries are picked self-assertively as given in the accompanying: \( M = 1; S = 2; \lambda = 1; Sc = 1; \sigma = 0.1; \text{Nb} = 0.5; \gamma = 0.1; \text{Nt} = 0.5; \text{Pe} = 1; \text{Pr} = 1; \text{Le} = 1; \text{Nr} = 0.5; \text{Nc} = 0.5 \). Further, in this segment we discussed the graphical consequences of the work of (Aman et al. [28]). The first order system of equation (7) to (10) together boundary and initial conditions (15) has been resolved by applying the appreciation ND solve on MATHEMATICA version 11. The computational results for velocity, concentration, temperature, and density function of motile micro-organism have been obtained for several interested parametrical values namely magnetic parameter, the injection/suction parameter, Stretching/Shrinking parameters.

The results have been presented in tabular form in Table 2. The impact of suction/injection at the wall on component of velocity, concentration profile, temperature profile, and profile of motile micro-organism.

#### 5.1. Velocity Distribution

In this section, we will confer certain flow parameters that are considered in the velocity contour in the form of schemes. The Hartmann number \( M \), section or injection parameter \( S \) are plotted against the velocity function \( f' \). The consequence of the parameter \( S \) on the velocity profile \( f' \) is shown in Fig. 3. As the parametric value of \( S \) increases, the curves show decreasing behavior. The impact of shrinking sheet parameter \( \lambda' \) is described in Figs. 4 and 5.
Table 2. Nusselt number, Sherwood number and local density number at the stretching walls.

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Figure 3. Distribution of velocity profile for some values of $S$.

Figure 4. Distribution of velocity profile for some values of $\lambda'$. The speed of flow is enhanced and reduced for increasing values of $\lambda'$ and $\lambda$ respectively. The sense of parameter $M$ on velocity profile of the fluid is demonstrated by Fig. 6.

Figure 5. Graph pattern of velocity profile for some values of $\lambda$.

Figure 6. Diagram of velocity profile for some values of $M$. 
These curves show reduction in velocity profile with the cumulative values of $M$. It is because of the cooperation of restricting powers, to be specific Lorentz power, which is expanded. The Lorentz power is a blend of electric and attractive powers on a moving point charge because of electromagnetic fields. Lorentz powers are resistive powers and are associated with attractive numbers. With the augmentation in, Lorentz power supports up, which goes against the fluid stream because of decrease in the speeds.

### 5.2. Temperature Distribution

In this section, parametrical effects of diffusivity ratio $Nbt$, Prandtl number $Pr$, chemical reaction parameter $\gamma$, magnetic parameter $M$, Lewis number $Le$, suction or injection parameter $S$, shrinking sheet parameter $\lambda'$, and parameter of heat capacity $Nc$ are depicted in Figs. 7-13. Behavior of temperature profile with reference to parameter $S$ is represented by Fig. 7. When there is gradual increase in the standards of suction or injection parameter $S$, curves of temperature profile depict deceleration behavior gradually. Fig. 8 illustrates the behavior regarding magnetic parameter on temperature profile.

![Figure 7. Diagram of temperature profile for some values of $S$.](image1)

![Figure 8. Diagram of temperature profile for some values of $M$.](image2)

The graph curves show significant increment in temperature profile with the increasing values of $M$. Fig. 9 shows the consequence of shrinking parameter $\lambda'$ on temperature profile. The decrease in the principles of $\lambda'$ in the stretching case resulted in reducing the temperature contour $\theta$. Fig. 10 is sketched to analyze the influence of Prandtl number $Pr$ on temperature profile, while keeping other parameters constant. Deceleration in temperature field was obtained when increment was done in values of $Pr$.

![Figure 9. Diagram of temperature profile for some values of $\lambda'$.](image3)

![Figure 10. Diagram of temperature profile for some values of $Pr$.](image4)

Fig. 11 is demonstrated to examine the effect of $Nc$ on the temperature profile. When the increment is done in the parametric value of heat capacity ratio, the curves of temperature profile gave an increasing behavior. So, temperature was increased with increasing the heat capacity ratio. Fig. 12 indicates the conduct of temperature profile with respect to parametric values of diffusivity ratio $Nbt$. When a gradual increment is done in the morals of diffusivity ratio $Nbt$, deceleration is obtained in the temperature field. Fig. 13 is drawn to summarize the consequence of Lewis number $Le$ on the temperature profile. The curve pattern shows that the increasing Lewis number markedly decreased the temperature profile.
5.3. Concentration Distribution

In this section, influences regarding diffusivity ratio parameter $N_{bt}$, chemical reaction parameter $\gamma$, magnetic parameter $M$, suction or injection parameter $S$, shrinking sheet parameter $\lambda'$ and Schmidt number $Sc$ are depicted on the concentration profile in Figs. 14-19. Fig. 14 displays the effect of stretching or shrinking sheet parameter on concentration profile. On increasing values of $\lambda'$, a decreasing behavior of concentration is obtained. In Fig. 15, diffusivity ratio parameter $N_{bt}$ is depicted to show its behaviour on concentration profile.

A significant downfall in the curve of concentration profile is obtained when gradual increase is done in diffusivity ratio parameter $N_{bt}$. Behavior of concentration profile regarding Schmidt number $Sc$ is depicted in Fig.16. When parametrical values of $Sc$ are boosted up, a significant decrease is resulted in concentration profile. Schmidt number is ratio between viscosity and molecular diffusion. Impact of chemical reaction parameter $\gamma$ on concentration profile is depicted in Fig.17.
Curve of concentration profile of fluid is decreased when chemical reaction parameter $\gamma$ is increased. The concentration profile curve with respect to magnetic parameter $M$ is demonstrated in Fig. 18. A remarkable increment is resulted in concentration field when magnetic field parameter is increased. The change in concentration profile for some values of suction or injection parameter $S$ is elaborated in Fig. 19. A decreasing behavior of concentration profile of fluid is obtained with increasing values of $S$.

5.4. Motile microorganism density Distribution

In this section, effects regarding Schmidt number $Sc$, Peclet number $Pe$, $\sigma$, and suction or injection parameter $S$ on the density profile of motile micro-organism are discussed in Figs. 20-23. Fig. 20 shows the effect of Peclet number $Pe$ on the density of motile microorganisms. It is observed that increment in the values of Peclet number is caused in increasing the density of motile microorganisms. Fig. 21 shows the effect of parametrical values of suction/injection on the density of motile microorganisms.
According to the plot, deceleration in density is attained for increasing values of S. The graph of Schmidt number $Sc$ on motile density profile is displayed in Fig. 22. Density profile of motile microorganisms is decreased for gradual increase in Schmidt number. Effect of dimensionless parameter $\sigma$ on density of microorganism is presented in Fig. 23. An important growth is observed in density, when dimensionless parameter $\sigma$ is increased.

6. CONCLUSION

The main objective is to understand the “radiative effects on MHD Williamson nanofluid flow over a porous stretching sheet with gyrotactic microorganism: Buongiorno's model”. Furthermore, the impacts of chemical reaction, magnetic effect and density of motile microorganism are under assumption. Firstly, useful dimensionless variables are implemented to alter the system of partial differential equations into system of ordinary differential equations. Later on, the approximate solution of transformed boundary value problem is calculated by using shooting scheme for numerically solution by employing ND solving command on Mathematica software. The effects of different physical parameters on non-dimensional velocity function, temperature profile, mass concentration profile and motile microorganism's density function are observed. The principal revelations of this work are as per the following:

- The effect of attractive field is to diminish every one of the actual amounts of interest, where it affected fundamentally on speed work.
- The speed of nanofluids diminishes by expanding attractions boundary $S$.
- The temperature nanofluids profile increments by expanding $Nc$.
- The temperature work for nanofluids diminishes by expanding Prandtl number $Pr$.
- The concentration function decreases by increasing $Nb$.
- The concentration function decreases by increasing $Sc$.
- The microorganism density is increased by collective bio convection Peclet number $Pe$

The shooting method could be applied to a variety of physical and technical challenges in the future [31-35].

Data Availability
All data generated or analyzed during this study are included in this published article.

Conflict of Interest
The authors announce that no conflict of curiosity exists.

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Bioconvection Effects on Non-Newtonian Chemically Reacting Williamson Nanofluid…


ВПЛИВ БІОКОНВЕКЦІЇ НА ПОТІК НЕНЬЮТОНІВСЬКОЇ ХІМІЧНО РЕАГУЮЧОЇ НАНОРІДИНІ ВІЛЬЯМСОНА ЧЕРЕЗ РОЗТЯГНУТУ ПОВЕРХНЮ З ТЕПІЛО-ТА МАСОПЕРЕНОСОМ

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Метою цієї статті є детальне дослідження зміщеного конвективного потоку нанорідини Вільямсона за навантаження та розтягнуту поверхні з різними фізичними ефектами. Вплив броунівського руху та термофорезу є частиною цього дослідження. Крім того, для мотивації проблеми в рівнянні енергії враховуються особливості теплового випромінювання. Для стабілізування моделі використовується теорія мікроорганізму. Проведено математичне моделювання. Відповідні функції подібності використовуються для перетворення пакету рівняння PDE в набір ODE. Wolfram MATHEMATICA займається чиселними вирішеннями трансформованих рівнянь за допомогою схеми зйомки. Вплив параметрів потоку, таких як магнітний, термофорез, пористість, число Пекле та Льюїса, на швидкість, температуру, об’ємну концентрацію та щільність розподілу мікроорганізмів представлено в таблицях і графіках.

Ключові слова: гідротехнічний мікроорганізм; нанорідина Вільямсона; МГД, біоконвенція; метод стрільби